

Accelerating Gaussian Processes and Deep Kernel Networks on GPUs

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NVIDIA GTC 2020, Startup Showcase

Gaussian Processes

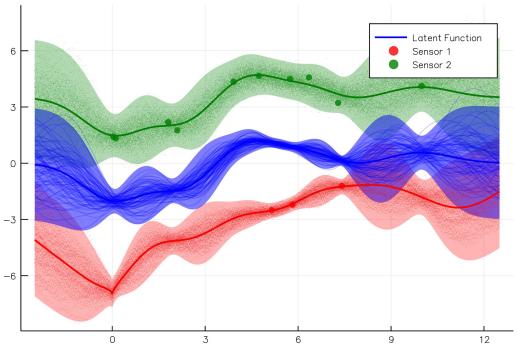
A Gaussian Process (GP) defines the distribution over the possible functions f(x) that are consistent with the observed data X.

Why GP?

- Very flexible, Bayesian nonparametric model for unknown functions
- Powerful for regression, classification, unsupervised learning, and other applications that require inference on functions
- Uncertainty reasoning and interpretability for free

Widely used across academia and industry

- Applications from disease modeling to climate predictions to financial modeling to robotics control...
- Well-supported libraries: GPyTorch, GPFlow, Stheno.jl, etc.



Example of using GPs for modeling noisy machine sensors.

Using Gaussian Process Models

The Automatic Statistician¹ is a tool that uses GPs and flexible kernels to automatically discover plausible models from time-series data.

Bayesian Optimization (BO): a class of approaches to black-box function optimization that typically utilizes a GP surrogate to model an expensive objective.

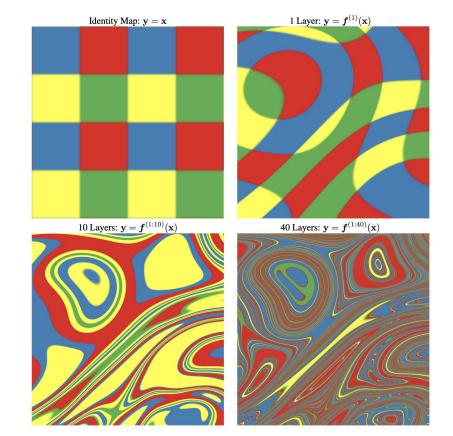
Deep-GP: deep neural networks as compositions of functions drawn from GP priors (right).

Models with GP-priors:

- GPPVAE³ to better model correlations in time-series data
- GPMP⁴ frames robot motion planning as probabilistic inference

But in general $O(N^3)$ inference and $O(N^2)$ space

... scaling is the common issue preventing wider utility!



Visualization of mapping of a two dimensional space through a deep Gaussian Process.²

- [2] Duvenaud et al. (2016) Avoiding pathologies in very deep networks: arxiv.org/abs/1402.5836
- [3] Casale et al. Gaussian Process Prior Variational Autoencoders. NeurIPS 2018.

[4] Dong et al. Motion Planning as Probabilistic Inference using Gaussian Processes and Factor Graphs. RSS 2016.

^[1] Zoubin Ghahramani et al.: automaticstatistician.com

How to accelerate and scale Gaussian Processes?

Sparse GPs are typically used in practice¹:

- Approximate the GP with m inducing points, yielding O(nm²) inference and O(nm) storage
- Variational methods optimally select inducing points
- Stochastic variational inference methods allows GPs to be fitted to millions of data with O(m³)

Can we utilize advances in ML hardware?

Deep learning can parallelize massive matrix computations on GPU, but the GP bottleneck is a different matrix operation, the Cholesky decomposition...

[1] Recommended papers on approximate / scaling GPs:

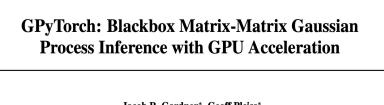
- Titsias. Variational learning of inducing variables in sparse Gaussian processes. AISTATS, 2009.
- Hensman et al. Gaussian processes for big data. UAI, 2013
- Hensman et al. .Scalable variational Gaussian process classification. ICML, 2015.
- Wilson et al. Thoughts on massively scalable Gaussian processes. arXiv:1511.01870, 2015.

Avoiding Cholesky to parallelize GPs on GPU

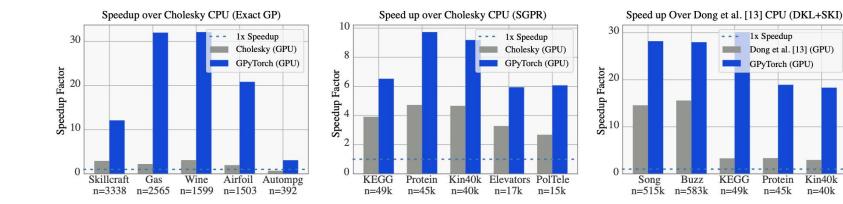
Blackbox Matrix-Matrix (BBMM) method,

- reduces the bulk of GP inference to highlyparallelizable matrix-matrix multiplication.
- reduces the time complexity of exact GP inference from $O(n^3)$ to $O(n^2)$.

Standard in GPyTorch library!



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[1] Garner et al. GPyTorch: Blackbox Matrix-Matrix Gaussian Process Inference with GPU Acceleration. NeurIPS 2018.

Challenging use-case: Deep Kernel Nets for Computer Vision

*Deep Kernel Learning (DKL)*¹ combines the structural properties of neural networks as feature-extractors, with the non-parametric flexibility of kernel methods (i.e. Gaussian processes).

For computer vision we can use:

- 1. ConvNet feature extractor (e.g. DenseNet)
- 2. GP regression layer on top

Yields near state-of-art on object classification tasks, with uncertainty reasoning!

Scalable inference on GPU via BBMM.

Moar? We can implement *probabilistic programmed* version by warping the GP and ConvNet into a new kernel.

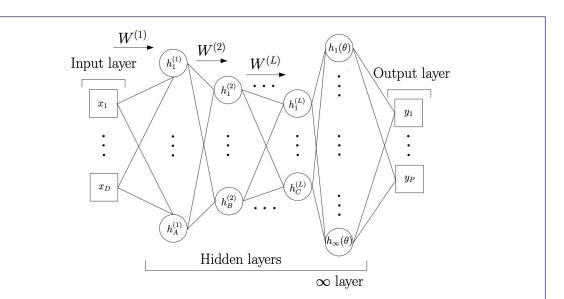


Figure 1: Deep Kernel Learning: A Gaussian process with a deep kernel maps D dimensional inputs **x** through L parametric hidden layers followed by a hidden layer with an infinite number of basis functions, with base kernel hyperparameters $\boldsymbol{\theta}$. Overall, a Gaussian process with a deep kernel produces a probabilistic mapping with an infinite number of adaptive basis functions parametrized by $\boldsymbol{\gamma} = \{\mathbf{w}, \boldsymbol{\theta}\}$. All parameters $\boldsymbol{\gamma}$ are learned through the marginal likelihood of the Gaussian process.

[1] Wilson et al. Deep Kernel Learning. AISTATS, 2015.

[2] van de Meent et al. (2018) An Introduction to Probabilistic Programming. arxiv.org/abs/1809.10756.

PyTorch + NVIDIA GPU Ecosystem makes this possible, *and useful in industry settings*



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Gregory Renard, Chief Al Officer

Renowned expert in NLP and knowledge graphs, decades of experience deploying augmented-intelligence products.

Alexander Lavin, Technical Fellow & Director of Research Former rocket scientist turned Al research engineer, leading expert in Bayesian machine learning.

Thank You

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